

# Advanced Bayesian Methods: Theory and Applications in R

Monitoring Mixing and Convergence

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#### Remarks

- Monitoring the mixing and convergence of Markov Chain Monte Carlo (MCMC) samples is crucial for reliable inference.
- Poor mixing or lack of convergence may result in biased parameter estimates or incorrect conclusions.
- Several diagnostic techniques and visual tools are available to assess mixing and convergence.

## Key Concepts in MCMC Diagnostics

- **Mixing**: How well the Markov chain explores the target distribution.
- **Convergence**: Whether the chain has reached the stationary distribution, i.e., the target posterior distribution.
- **Burn-in**: Initial samples may not represent the stationary distribution and are usually discarded.
- Effective Sample Size (ESS): Indicates how independent the samples are.

#### **Trace Plots**

- A trace plot shows the values of the parameters over iterations.
- Well-mixing chains should exhibit random fluctuations around a stable mean.
- Poorly mixing chains may show strong autocorrelation or trend.



### Autocorrelation Function (ACF)

- The ACF of a parameter indicates how correlated the samples are at different lags.
- If the ACF decays quickly, the chain is well-mixed.
- Slow decay indicates strong autocorrelation, which reduces the effective sample size.

## Effective Sample Size (ESS)

- Effective sample size is a measure of how many independent samples your chain has.
- High autocorrelation leads to lower ESS, meaning fewer independent samples.
- ESS can be calculated in R using the *coda* package.

# R Example: Effective Sample Size

### Gelman-Rubin Diagnostic (R-hat)

- The Gelman-Rubin diagnostic compares the variance within chains to the variance between chains.
- $\hat{R}$  close to 1 indicates convergence.
- $\hat{R}$  values significantly greater than 1 suggest lack of convergence.

# R Example: Gelman-Rubin Diagnostic

Calculate  $\hat{R}$  using the *coda* package.

```
R> library("coda")
R> gelman_diag <- gelman.diag(samples(b, combine = FALSE))</pre>
```

#### Conclusion

- Monitoring the mixing and convergence of MCMC samples is crucial for obtaining reliable estimates.
- Key diagnostics include trace plots, autocorrelation, effective sample size, and the Gelman-Rubin diagnostic.
- R provides useful tools for performing these diagnostics.